



ttp://ieeexplore.ieee.org/Xplore

# A Multicast Technique for Fixed and Mobile Optical Wireless Backhaul in 5G Networks

Michael Atakora, Member, IEEE, and Harsha Chenji, Member, IEEE

Abstract—The data demand for 5G networks is expected to be much higher than current throughput requirements. To meet this demand, a dense topology of interlinked small cells is needed. Laying new copper and fiber in such a dense network would be cost prohibitive. There is therefore an urgent need for high capacity wireless point-to-multipoint backhaul solutions. In this paper, we provide a compendium of solutions for ultra high data rate physical layer broadcast and multicast using free space optics in 5G backhaul networks. We show that the problem of optimal multicast in mobile scenarios with highly directional optical links is a time-dependent prize collecting traveling salesman problem which is NP-hard. In formulating our problem we develop a novel prize assignment strategy that guarantees the selection of mutually non-disjoint multicast sets. Due to the problem being NP-hard, we provide several potential heuristics for multicast in fixed and mobile scenarios, and present a comprehensive performance evaluation of the developed schemes.

*Index Terms*—Free space optics, multicast, 5G, backhaul, set cover, traveling salesman problem.

#### I. INTRODUCTION

The upcoming 3GPP 5G standard is designed to provide several gigabits per second throughput to users. The recent availability of several GHz of spectrum in the millimeter wave range is a key enabler of this throughput. 5G networks are envisioned to have a node density of about 50 BSs/km<sup>2</sup> [1]. This densification of cellular networks, combined with high throughput links, leads to interference. In order to manage interference and to ensure coverage in indoor and challenged environments, the concept of femto-, atto-, pico-cells and several other small cells have been proposed. However, these cells need to be interlinked - and the cost of laying new fiber or copper is extremely high. Therefore, there is an urgent immediate need for high capacity wireless backhaul solutions. These backhaul links cannot be fixed point-to-point wireless, but they need to support point-to-multipoint (using beam steering or other techniques) to accommodate Quality of Service and other constraints.

The 3GPP standards for LTE specify the Evolved Multimedia Broadcast and Multicast Service interface; it is anticipated that the corresponding demand in 5G will be much higher. Another interesting application of high data rate wireless point-to-multipoint communication is in datacenters where fiber is replaced by laser-based free space optical (FSO) links [2], [3]; data replication occurs in applications such as MapReduce and redundant storage. In mobile delay tolerant

M. Atakora and H. Chenji are with the School of Electrical Engineering and Computer Science, Ohio University, Athens, OH 45701, USA email: ma136412, chenji@ohio.edu. Earlier version of this article appeared at Globecom 2016 and IWCMC 2017. We gratefully acknowledge the funding provided by the National Science Foundation under CNS-1657279.

Manuscript submitted February 28, 2018.

Digital Object Identifier: 10.1109/ACCESS.2018.2832980

networks [4], replicating a packet to multiple nodes during a contact opportunity is very important.

While mmWave backhaul links have been investigated, we propose the use of FSO links for several reasons. First, compared to mmWave (tens of milliradians), the beamwidth is much smaller ( $\mu$ rad range) and therefore supports higher densification. Second, the entire optical spectrum is license free, with several THz of freely available spectrum. Third, inexpensive commercial off-the-shelf equipment can be used to establish multi-Gbps FSO links (e.g., Koruza [5]). This development is largely due to the availability of cheap fiber optic communication hardware - FSO links can be established by removing the optic fiber cable [6]. Fourth, laser communication has been demonstrated [7] at distances exceeding 100km, and at bit rates exceeding 80Gbps (though not simultaneously) in both static and mobile scenarios. In fact, the NASA LLCD project recently demonstrated an Earth-Moon optical link. These success stories continue to happen: Facebook very recently demonstrated an 80 Gbps, 13 km free space optical cross-link designed for use as backhaul in platforms such as OpenCellular.

Laser data rates are very high mainly because the beamwidth is very small [8]. Trying to reduce the link alignment time by widening the beam has the unwanted side effect of heavily reduced data rate. Thus there is a fundamental tradeoff between data rate and alignment delay. This problem is not very apparent in point-to-point links where the latter is incurred only once when the link is initially setup. Unfortunately this delay is incurred *multiple times* in backhaul networks where senders frequently talk to multiple receivers (e.g., during broadcast). In such networks it is essential to address this problem before trying to improve capacity by deploying highly directional links.

Motivated by the need for multimedia broadcast and multicast at ultra high data rates, we investigate the problem of physical layer multicasting (as opposed to multicast routing) in free space optical networks. We expand upon our previous work on FSO multicast in static scenarios [9] and emulated static conditions in mobile delay tolerant networks [4], [10]. While static multicast was shown to be NP-hard through reduction to Set Cover, we show that mobile multicast is an instance of the Time-Dependent Prize Collecting Traveling Salesman problem. The rest of this paper is organized as follows: we put our work in context with related efforts and present scenarios in which our developed solutions can be applied to in Section II. In Section III, we present a brief review of performing optimal multicast in static environments, whiles mobility is covered in Section IV. In Section V, drawing from our solutions for static and mobile scenarios, we compare solutions for both scenarios, and the effectiveness of using



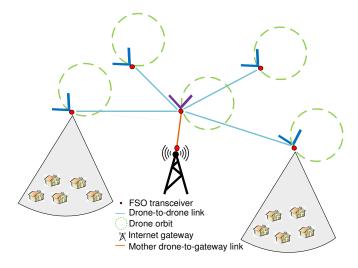


Fig. 1: Possible application of mobile multicast: A high altitude platform for Internet access in rural communities.

one solution for an environment it was not designed for. In the same section, we formulate heuristics meant to support mobile multicast. An evaluation of the various multicast schemes is presented in Section VI, after which we provide a conclusion.

#### II. APPLICABLE SCENARIOS & RELATED WORK

Multicasting in directional networks (whether RF, mmWave or optical) has been investigated in the state of art. In this section we first describe our application scenario (5G backhaul) through the use of expository examples, and summarize past and ongoing work. Static and mobile scenarios are differentiated and described in detail. Then, we provide a summary of related work across the spectrum, and show that our work is unique in several aspects. Contributions of this article are summarized, and is differentiated from our previous work [9], [4], [10].

## A. Applicable Scenarios

We now present some scenarios in which multicast can be used when nodes are either static or mobile.

Static Multicast:- With the ever growing demand for data traffic, 5G and other next generation wireless systems, cannot completely rely on macro cells to support the increase in data capacity. A dense deployment of small cells having a range of at most a few hundred meters is widely recognized as the direction to proceed in addressing increasing data capacity demands [11], [12], [13]. A major challenge that has to be confronted with such a dense deployment of small cells is the provision of a backhaul network connecting these cells to the core network. Obviously, a wired backhaul would not only be expensive, but would also be unscalable [14], [15], [16]. There is therefore the need to make provision for a cost-effective and scalable backhaul network that does not use the already congested sub 3 GHz portion of the electromagnetic spectrum. In [15], [17], [18], the use of millimeter-wave (mmWave) backhaul links in the unlicensed 60 GHz band and licensed 70 to 80 GHz band between macro and picocells and among picocells has been explored. With mmWave backhaul systems, data is aggregated from multiple users within the coverage area of a small cell's base station (S-BS) and routed via multiple high capacity mmWave backhaul links to the macrocell's base station (M-BS) which then forwards it to the core network. Point to multipoint backhaul networks [15], [17], [18], [19], [20] allow for a low latency and cost effective 5G inter-BS reconfigurable wireless backhaul since any required link can be created on demand by virtue of either beam steering or beam switching as opposed to setting up  $\mathcal{O}(n^2)$  dedicated links to connect n BSs. The use of hybrid RF/FSO as a backhaul solution for 5G wireless systems has been investigated [21], [22], [23]. Multicast can be leveraged in improving the latency and throughput of high capacity wireless optical backhaul networks for 5G communications and other next generation technologies.

Mobile Multicast:- In networks with highly directional transceivers, mobility introduces challenges with respect to maintaining links during a communications period. Pointing, acquisition, and tracking of the optical beam needs to be precise so as to preserve the link's existence. Facebook's plan to beam the Internet to rural and hard to reach areas using laser equipped solar powered drones [24], [25], [26] is a possible scenario whereby multicasting can improve throughputs. The basic concept of Facebook's proposed approach is presented in Figure 1. A network is formed between high altitude drones linked to a ground based Internet gateway via a "mother" drone. The drones relay Internet payload between themselves using high speed optical links and they serve their target communities with Internet via radio.

## B. Related Work

Over the last few years, many researchers have explored areas such as highly directional multicasting and wireless optical mobile ad-hoc networks. In this section, we present these related efforts and compare how they differ with the work presented in this paper.

The multicast problem in energy-aware and energy-limited RF networks is addressed in static scenarios using tree construction algorithms [27], [28], [29], [30], [31], [35], [36], [37], [38], [39], [40], [41], [42], [43], [44]. These efforts do not tackle mobility. Optimal link layer multicasting in indoor static RF wireless networks using antennas with switched beamforming capabilities is achieved in [88] by manipulating the power across the composite beam's main lobes. For static mmWave wireless networks, [45] proposes an adjustable beamwidth mechanism which maximizes the data rate of receiving nodes. In the area of directional multicast in RF-based adhoc networks, the approach in [32], [33], [34] and [84], [85] use switchable antennas with fixed patterns in mobile and static environments respectively. The use of directional antenna systems in vehicular networks has been widely studied [75], [82], [83], [70]. The authors of [75] study the multicast throughput capacity in directional RF antenna based vehicular ad hoc networks subject to delay constraints. Using a linear highway vehicular mobility model, a protocol for the dissemination of broadcast data from a static base

TABLE I: Summary of related research efforts

Paper	Optical	Directional Multicast	Tracking	Steerable	Switchable	Single Active Directional Beam (Antenna Element)	Adjustable Beamwidth	Mobility
[27], [28], [29], [30], [31]		<b>√</b>		<b>√</b>			<b>√</b>	
[32]		✓	<b>√</b>		<b>√</b>	✓		<b>√</b>
[33], [34]		✓	√		<b>√</b>			<b>√</b>
[35], [36], [37], [38], [39], [40], [41], [42], [43], [44]		<b>√</b>		<b>√</b>		<b>√</b>	<b>√</b>	
[45]		✓		<b>√</b>			✓	
[46], [47], [48], [49], [50], [51], [52], [53]	<b>√</b>		<b>√</b>	<b>√</b>		<b>√</b>		<b>√</b>
[54], [55], [56], [57], [58], [59], [60], [61], [62], [63], [64], [65]	<b>√</b>		<b>√</b>		<b>√</b>			√ 
[66], [67], [68], [69]	<b>√</b>		<b>√</b>	<b>√</b>				<b>√</b>
[70]			✓		<b>√</b>			✓
[71]				<b>√</b>		✓		
[72]	✓						✓	
[73]		✓		✓		✓		
[74], [75]		✓	✓	✓		✓		✓
[76]				✓		✓		
[77]					<b>√</b>			
[78], [79]			<b>√</b>		<b>√</b>			✓
[80]				<b>√</b>	<b>√</b>	<b>√</b>		
[81]			✓	<b>√</b>	✓	<b>√</b>		<b>√</b>
[82], [83]		<b>√</b>				✓		✓
[84], [85]		<b>√</b>			<b>√</b>			
[86]		<b>√</b>			✓	✓		
[87]		<b>√</b>	✓					✓
[88]		✓		✓	<b>√</b>		✓	
Our work	✓	✓	✓	✓		✓	$\checkmark$	✓

station along the road to mobile vehicles is developed [82]. The protocol incorporates a mechanism to select relay vehicles in a manner that maximizes broadcast throughput.

In [54], [55], [56], [57], [58], [59], [60], [61], [62], [63], the authors introduce and implement a FSO node design in which spherical surfaces are tessellated with several transceivers to attain near omnidirectional node coverage. They achieve this by means of an auto-alignment circuit that detects a loss of line of sight by electronically tracking optical beams. These efforts use LEDs which have divergence angles far greater than that of lasers used in our work. Using the tessellated transceiver design, [64], [65] design a distance vector routing protocol for hybrid RF/FSO based mobile adhoc networks. An evaluation of the impact of directional communications on ad hoc networks running dynamic source routing is presented [74].

The issue of link maintenance [46], [47], [48], [49], [50], [51], [52], [53] in wireless optical mobile networks, although addressed, is limited to just a pair of nodes. In [51], [52], inclinometer sensors and GPS are used to obtain a node's position for coarse alignment, whiles [46], [47], [48], [49], [50] uses an inband approach comprising of directional transceivers sending beacon signals to achieve the same objective. [53] explores improving connectivity using adaptive divergence and transmit powers. With respect to RF, [70] explores using beam steerable directional antennas to improve link stability between

mobile vehicles and a static base station.

The issue of medium access control (MAC) in RF-based directional wireless networks has been well investigated [73], [76], [77], [78], [79], [87]. [73], [76] explores and addresses challenges in MAC protocol design stemming from interference due to the higher ranges of directional transmissions. The authors of [87] develop a TDMA-based MAC protocol that maximizes the number of concurrent sessions in the network. For the improvement of the lifetime of an ad hoc wireless network, coordination of transmissions is required. In [71], this is made possible using electronically steerable directional antennas to develop an energy-efficient routing and scheduling algorithm.

The authors of [66], [67], [68], [69] develop algorithms for unicast networks with fragile optical links. The objective of such algorithms is the minimization of a transient information level metric defined to be a function of both the amount of information in the network and the projected physical distance to the destination, where constraints such as Quality of Service (QoS), varied network traffic, transmission and storage limits are incorporated into the algorithm. To meet QoS requirements such as latency and throughput, adaptive control of power and beamwidth is explored in [72] for topology control in hybrid RF/FSO mesh networks.

We draw from a number of concepts such as the ability

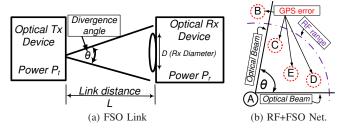


Fig. 2: (a) Illustrating various FSO link parameters for a point-to-point link:  $P_t, P_r, L, \theta$  and D. (b) A RF+FSO network where A talks with C, D & E with a FSO beam divergence of  $\theta$ . A is unaware of B since it is outside of A's RF radio range.

to perform directional multicasting, usage of a single directional steerable transceiver, the adjustment of beamwidth and mobility in building our multicast algorithms in highly directional optical networks. In Table I, we categorize related efforts using the concepts we build on in our work. We indicate which concepts or techniques were used (with a ✓). In Table I, optical refers to the use of wireless optical transceivers such as LEDs and lasers, directional multicast refers to using multicasting in directional networks as opposed to performing omnidrectional broadcast, tracking refers to the ability for the transmitted beam to follow the trajectory of mobile nodes, steerable refers to using a single transceiver which can be guided to point in any direction, rather than a switchable antenna system whereby the direction in which the antenna system points to can be manipulated by changing which antenna is active. A single directional beam means that, there is only one active beam per transmitter whiles the adjustable beamwidth category refers to the ability to change the beamwidth of the transceiver on the fly.

Our main contributions in this paper is the development of a compendium of solutions for multicast over free space optical links in static and mobile scenarios. We expand upon our previous work on FSO multicast in static scenarios [9] and emulated static conditions in mobile delay tolerant networks [4], [10]. This effort is different from our work in [9], [4], [10] mainly due to the consideration of mobility. In this paper (Section IV) we provide a generalized solution for achieving optimal multicast in *mobile* networks via a translation of the problem to the Time-Dependent Prize Collecting Salesman Problem.

#### III. OPTIMAL MULTICAST: THE STATIC SCENARIO

In this section we review our static multicast algorithms from [9], [10]. We provide a background into the FSO PHY, describe concepts such as broadcast and multiple unicast which ultimately lead us to formulating the static FSO multicast problem. We then provide an exact solution and a faster but approximate greedy heuristic.

## A. Preliminaries

The beam generated at the FSO source either diverges due to physical imperfections in the source, or can be made to diverge using a lens; this angle of divergence is defined as the beam divergence angle  $\theta$  (Figure 2a). Given L as the Euclidean distance between the sender and receiver, the effective data rate  $R_b$  at a divergence angle of  $\theta$  is expressed [89] as

$$R_b(\theta) = \frac{P_r}{hfN_b} = \frac{P_t D^2 L_{tp} L_{rp} \eta_t \eta_r 10^{\frac{-\alpha L}{10^4}}}{hfN_b \theta^2 L^2}$$
(1)

where  $P_t$  is the transmitted power, D is the receiver diameter,  $L_{tp}$  and  $L_{rp}$  are the pointing losses resulting from imperfect alignment of the transmitter and receiver respectively,  $\eta_t$ and  $\eta_r$  are the transmitter and receiver optical efficiencies respectively,  $\alpha$  is the atmospheric attenuation factor, f is the frequency of the light source, h is Planck's constant and  $N_b$  is the detector sensitivity. The RF+FSO system model is shown in Figure 2b. The nodes ("A,B,C,D,E" in Figure 2b) are equipped with an omnidirectional RF radio as well as a directional FSO radio. Nodes broadcast their position over RF. We account for possible positioning errors (dotted line around nodes in Figure 2b), since GPS systems currently have a 3m position accuracy g 95% of the time. Therefore, nodes have to set  $\theta$  such that the receiver is within the FSO footprint. Nodes outside the RF range ("B" in Figure 2b) are not considered as neighbors since their location cannot be obtained.

#### B. System Model: Broadcast vs. Multiple Unicast

The fundamental building blocks to formulating the static multicast problem are the concepts of broadcast and multiple unicast which are based on the ability to manipulate beam divergence and steer the laser transmitter. With broadcast (Figure 3a) the transmitter's  $\theta$  is manipulated so that all receivers are within its footprint. In the case of multiple unicast (Figure 3b), data is sent to each receiver one at a time with non-zero alignment delay  $d_{al}$  accounted for. We define  $d_{al}$  as the time it takes a node to perfectly reorient it's laser transmitter in the direction of another node. We use our understanding of broadcast and multiple unicast to obtain all possible multicast combinations. We define a universe  $\mathcal{U}$  of nodes that are to receive broadcast data. A set  $S_i$  is a group of nodes in the network whereby exactly one transmission is required to multicast to each of it's elements. It is noted that the union of all sets  $S_i$  should be equal to  $\mathcal{U}$ . A hybrid combination of sets is presented in Figure 3c whereby the first multicast transmission is a broadcast to B & C with the second transmission being a unicast to D.

The minimum number of multicast sets K can be derived by sorting receivers in order of decreasing azimuth  $\phi$  from the origin (where node A is located) and observing that, whiles following a clockwise trajectory, if  $\phi_i$  for node i is less than  $\phi_j$  for node j, and greater than  $\phi_k$  for node k, and if  $j, k \in S_x$ , then node  $i \in S_x$ . Using this structure to enumerate all possible sets for a given  $\mathcal{U}$  from Figure 3, we see that there is exactly 1 set of size 3  $(S_1)$ , exactly 3 sets of size 1  $(S_2, S_3, S_4)$ , and exactly 3 sets of size 2  $(S_5, S_6 = \{C, D\}$  and  $S_7 = \{D, B\}$ ,  $S_6$  &  $S_7$  are not shown in Figure 3). Therefore generally, to broadcast to N nodes, there are exactly N sets of size 1 through to size N-1, and exactly 1 set of size N, for a total of  $K = N^2 - N + 1$ . The constructed sets lead us to the static FSO multicast problem (S-FSOMP).

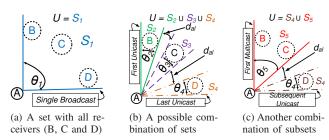


Fig. 3: Illustrating several set combinations in FSO multicast (a) a broadcast set with a FSO beam divergence angle of  $\theta_1$  (b) multiple (three) unicasts with divergence angles of  $\theta_2$ ,  $\theta_3$  and  $\theta_4$  (c) a hybrid of broadcast and unicast sets. The union of all sets in a diagram is always equal to the universe of nodes.

### C. Static Multicast Problem Formulation

The static FSO multicast problem can be stated as follows: given a universe  $\mathcal{U}=\{n_1,n_2,\ldots,n_N\}$  of N nodes, a collection  $\mathcal{S}=\{S_1,S_2,\ldots,S_K\}$  of  $K=N^2-N+1$  sets can be constructed. The cost of broadcasting data to a set  $S_i$  is the data delivery delay  $d_i$  which depends on  $R_b$  for that set, which in turn depends on the required  $\theta$ . The objective is to find  $\mathcal{S}'\in\mathcal{S}$  with minimum total delay such that all N nodes are covered. The delivery delay  $d_i$  for a set  $S_i$  is computed using the size of the broadcast data P, the minimum divergence angle  $\theta_i$  required for all member nodes to be in the transmitter's footprint, and alignment delay  $d_{al}$ . Using Equation 1,  $d_i$  is calculated as

$$d_i = \max_j \left\{ \frac{P}{R_b(\theta_i)} + d_{al} \right\} \text{ where } 1 \le j \le |S_i| \qquad (2)$$

where  $R_b(\theta_i)$  is calculated for each node  $j \in S_i$  using different values of distance  $L_j$ . We formulate the optimal FSO multicast problem as a 0/1 integer problem. Each set  $S_i$  is assigned a binary decision variable:  $x_i$  is 1 if  $S_i \in \mathcal{S}'$ , and 0 otherwise. The problem can now be formulated as follows.

Problem 1. The Static FSO Multicast Problem

minimize 
$$\sum_{i=1}^{K} x_i d_i$$
 (3)  
subject to 
$$\bigcup S_j = \mathcal{U} \quad \forall \quad S_j \in \mathcal{S}'$$
 (4)

subject to 
$$\bigcup S_j = \mathcal{U} \quad \forall \quad S_j \in \mathcal{S}'$$
 where  $S_i \in \mathcal{S}'$  if  $x_i = 1$ 

In the objective (Equation 3), the delay  $d_i$  per set is the cost (Equation 2) of sending data to all nodes in that set. Equation 4 stipulates that each node has to be in at least one set. Taking into account the structure of constructed multicast sets, we see that that optimal solution to S-FSOMP consists of mutually disjoint sets (see Theorem 1).

## D. The Exact Static Multicast Solution (S-SC)

We translate the Static FSO Multicast Problem (S-FSOMP) into a Minimum Weighted Set Cover (MWSC) problem. Formally, the MWSC problem is as follows. Given a universe  $\mathcal{U}$  of N elements, and a collection  $\mathcal{S} = \{S_1, S_2, \ldots, S_K\}$  of sets whose elements are in  $\mathcal{U}$ , where each set  $S_i$  is assigned

**Algorithm 1:** The Approximate Set Cover Algorithm (S-AP)

```
Input: A universe S = \{S_1, S_2, \dots, \overline{S_K}\} of K = N^2 - N + 1
     Output: A subcollection of sets S' that covers the universe of
                      \mathcal{U} = \{n_1, n_2, \dots, n_N\} of N nodes
  1 \mathcal{S}' \leftarrow \emptyset
 2~\mathcal{U}' \leftarrow \emptyset
 3 for S_j \in \mathcal{S} s.t. j \leftarrow 1 to K do
     compute d_j using Equation 2
 j^* = \min_{i} \frac{d_j}{|S_i|}
 6 \mathcal{S}'_{\underline{\cdot}} \leftarrow \overset{\jmath}{S_{j^*}}
 7 \mathcal{U}' \leftarrow \vec{S}_{i}^*
 8 while \mathcal{U}^{'} \neq \mathcal{U} do
            10
            j^* = \min \tfrac{d_j}{|S_i|}
11
            \mathcal{S}' \leftarrow \mathcal{S}' \bigcup S_{j^*}
\mathcal{U}' \leftarrow \mathcal{U}' \bigcup S_{j^*}
12
```

a weight  $w_i$ , the objective is to find a subset S' of S with minimum total weight such that each element in U exists in at least one set in S' (i.e., all elements are "covered"). We can easily see that S-FSOMP is equivalent to the MWSC problem.

**Theorem 1.** The exact minimum weighted set cover (MWSC) solution to S-FSOMP guarantees the selection of mutually disjoint multicast sets.

*Proof.* Suppose for the sake of contradiction that there exists a sequence of multicast transmissions  $\mathcal{D} = \{D_1, D_2, \dots, D_K\}$ with optimal total cost  $C(\mathcal{D})$  which contains a pair of mutually non-disjoint sets  $(D_1, D_2)$ . We let  $\theta_{D_1}$ ,  $C(D_1)$  and  $\theta_{D_2}$ ,  $C(D_2)$  represent the divergence angle and cost associated with sending data to sets  $D_1$  and  $D_2$  respectively. In addition, we let  $D_{12} = D_1 \cap D_2$ , and form two new sets  $F_1$  and  $F_2$  s.t.  $F_1 = D_1 - D_{12}$  and  $F_2 = D_2$ .  $F_1$  and  $F_2$  have  $\theta_{F_1}$ ,  $C(F_1)$  and  $\theta_{F_2}$ ,  $C(F_2)$  as divergence angle and cost respectively. A new sequence of disjoint multicast transmissions  $\mathcal{F} = \{F_1, F_2, \dots, F_K\}$  is created from  $\mathcal{D}$  s.t.  $F_i = D_i$ when  $i \geq 3$ . With the structure of multicast sets obtained via the azimuthal ordering of receivers, we see that  $\theta_{F_1} < \theta_{D_1}$ . Since  $C(S_i) \propto \theta_{S_i}^2$ ,  $C(F_1) < C(D_1)$ , hence  $C(\mathcal{F}) < C(\mathcal{D})$ . Since there is a sequence of disjoint multicast sets  $\mathcal{F}$  whose total cost is guaranteed to be smaller than  $\mathcal{D}$ , we establish the contradiction that  $\mathcal{D}$  represents an optimal solution.

## E. The Approximate Static Multicast Solution

The approximate solution S-AP to the static free space optical multicast problem is based on the standard  $O(\log N)$  set cover approximation algorithm in [90]. We present the solution in (Algorithm 1).

S-AP takes as input the collection of all K sets. The set cover is initially empty as seen in lines 1, and 2. In line 4, the cost effectiveness  $\frac{d_j}{|S_j|}$  of selecting a set  $S_j$  into the cover is initialized. S-AP works by greedily picking the most cost-effective set (smallest cost per uncovered set elements) in each

Algorithm 2: Greedy Local Optimum Heuristic (S-HEU)

```
Input: Location (x_i, y_i) for nodes n_1 to n_N, P, d_{al} Output: Sets containing nodes in multicast group

1 for i \leftarrow 1 to N do

2 \left\lfloor \phi_i \leftarrow tan\left(\frac{y_i - y_0}{x_i - x_0}\right) \right\rfloor

3 Sort nodes in clockwise order of \phi_i to obtain n_{1'} to n_{N'}

4 j \leftarrow 1

5 S_j \leftarrow n_{1'}

6 for i \leftarrow 1 to N' - 1 do

7 \left\lfloor \text{if } d_{i',i'+1} < d_{i'} + d_{i'+1} + d_{al} \text{ then} \right\rfloor

8 \left\lfloor S_j \leftarrow S_j \bigcup n_{i'+1} \right\rfloor

9 else

10 \left\lfloor j \leftarrow j + 1 \right\rfloor

11 \left\lfloor S_j \leftarrow n_{i'+1} \right\rfloor
```

iteration till all nodes are covered. In lines 6, 7, the most cost effective set is chosen into the cover. Whiles all nodes are not covered (lines 8 - 13), the cost effectiveness of a set is updated to reflect the cost associated with currently uncovered nodes (line 10). The most cost effective set is then placed in the cover. This process continues until all nodes are covered. This algorithm has a time complexity of  $O(N^2)$  if linear search is used to obtain the most cost effective set relative to covering previously uncovered nodes.

**Theorem 2.** The approximate minimum weighted set cover (S-AP) solution to S-FSOMP guarantees the selection of mutually disjoint multicast sets.

Proof. Suppose for the sake of contradiction that Algorithm 1 selects a pair of mutually non-disjoint sets  $(S_1, S_2)$  from the collection S of K multicast sets. We let  $\theta_{S_1}$ ,  $C(S_1)$  and  $\theta_{S_2}$ ,  $C(S_2)$  represent the divergence angle and cost associated with sending data to sets  $S_1$  and  $S_2$  respectively. We further assume that Algorithm 1 picks  $S_1$  first. In other words,  $S_1$  is the most cost effective set in lines 4 - 7. For the sake of simplicity, we assume that  $S_2$  is picked immediately after  $S_1$ . In addition, we let  $S_{12} = S_1 \cap S_2$ , and form a new set  $F_1$  s.t.  $F_1 = S_2 - S_{12}$ with  $\theta_{F_1}$ ,  $C(F_1)$  as divergence angle and cost (Equation 2) respectively. With the structure of multicast sets obtained via the azimuthal ordering of receivers, we note that  $F_1 \in S$ . With  $S_2$  containing at least all nodes in  $F_1$ , we observe that  $\theta_{S_2} > \theta_{F_1}$  which translates to  $C(F_1) < C(S_2)$ . In addition to this, it is clear that after  $S_1$  is picked,  $|S_2 - S_1| = |F_1 - F_2|$  $S_1$ . Therefore  $S_2$  cannot be picked in the next iteration since  $\frac{C(S_2)}{|S_2-S_1|} > \frac{C(F_1)}{|F_1-S_1|}$ . This process can be repeated for any pair of selected sets. We have thereby established via contradiction that Algorithm 1 always yields mutually disjoint sets.

Due to the computational complexity associated with the integer program formulation of the problem and the  $O(N^2)$  S-AP(Algorithm 1), these solutions might not be ideal for highly dense mobile networks where the network topology changes frequently. We therefore provide a greedy heuristic (Algorithm 2). The heuristic builds sets by greedily comparing the cost of broadcasting to that of multiple unicast to a pair of adjacent nodes. The delay  $d_{i',i'+1}$  associated with broadcasting to a pair of adjacent nodes  $n_{i'}$  and  $n_{i'+1}$  is

defined as the weight d (Equation 2) of a set  $S = \{n_{i'}, n_{i'+1}\}$ . Similarly, the delay  $d_{i'}$  associated with unicasting to a node  $n_{i'}$  is defined as  $P/R_b(\theta_{i'})$ . In lines 1 to 3, the sender sorts the receivers in clockwise order of azimuth  $\phi_i$  from the origin (sender's location). A set is then created and the first node in the array of sorted nodes is placed in it (lines 4,5). In lines 6 to 11, the algorithm compares the delay associated with broadcasting to a pair of adjacent nodes to that of multiple unicast. Nodes are placed in sets depending on which scheme is cheaper (lines 8-11).

#### IV. OPTIMAL MULTICAST: THE MOBILE SCENARIO

In Section III, we considered only instances where nodes where static and it was assumed that the sender of the multicast data was known, with all receivers pointing in the direction of the sender. Mobility introduces complexity into the design of multicast algorithms for mobile networks, hitherto not associated with multicast in static environments. With mobility, the cost associated with sending data to nodes in a set is a function of time. This is because  $R_b$  is no longer constant, but depends on time varying  $\theta$ ,  $\theta(t)$  and time varying transmitter to receiver distances L(t). In addition to identifying the sets to use for multicast, the order of consecutive transmissions also has an effect on the optimality of the multicast solution. The FSO Multicast Problem with Mobility (M-FSOMP) can be stated as follows: given a universe  $\mathcal{N} = \{n_1, n_2, \dots, n_N\}$  of N nodes, a collection  $S = \{S_1, S_2, \dots, S_K\}$  of  $K = N^2 - N + 1$ sets can be constructed. The cost of broadcasting data to a set  $S_i$  is the data delivery delay  $d_i$  which depends on a time varying  $R_b$  for that set, which in turn depends on the required  $\theta(t)$ . The objective is to find an ordered sequence of disjoint transmissions  $S' \in S$  with minimum total delay such that all N nodes receive broadcast data.

## A. The Time-Dependent Prize Collecting Traveling Salesman Problem (TDPCTSP)

We show that an instance of M-FSOMP can be translated into a Prize Collecting Traveling Salesman Problem (PCTSP) [91], [92], [93] with time-dependent edge weights. The time-dependence of edge weights gives rise to the Time-Dependent Prize Collecting Traveling Salesman Problem (TD-PCTSP). Formally TDPCTSP is stated as follows. Given a list of cities, a prize  $w_l$  at city l to be collected if visited, a penalty  $h_l$  if city l is not visited, and a time-dependent cost  $c_{uv}(t)$  between cities u and v, the objective is to find a tour of a subset of these cities such that the total cost and penalty is minimized, subject to the collection of a certain prize  $w_T$ .

In constructing the TDPCTSP instance, we create K+1 "virtual" nodes. The first virtual node  $v_0$  is the origin of the cycle (i.e. the sender of broadcast data in M-FSOMP). Each of the remaining K virtual nodes correspond to a unique multicast set in  $\mathcal{S}$ . In other words, we represent sets as virtual nodes in the TDPCTSP instance. The universe of virtual nodes  $\mathcal{V} = \{v_0, v_1, v_2, \ldots, v_K\}$  excluding the origin  $v_0$  maps directly to the collection of multicast sets  $\mathcal{S} = \{S_1, S_2, \ldots, S_K\}$  (i.e.  $v_1$  corresponds to  $S_1$ ,  $v_2$  corresponds to  $S_2$ , ...,  $v_K$  corresponds to  $S_K$ ). In broadcast networks, data replication

to the same node, apart from scenarios whereby a packet does not reach its next hop needs to avoided since it represents a wastage of network resources. With this in mind, the optimal solution to the M-FSOMP has to consist of mutually disjoint multicast sets. To ensure that all receiving nodes get broadcast data exactly once during a session, the trick in the TDPCTSP instance is to develop a prize assignment strategy that guarantees that all valid tours have the same unique total prize, whiles invalid tours have a prize not equal to the prize of any valid tour.

**Definition 1.** A valid tour  $\mathcal{T}$  is a cycle of  $\mathcal{V}' \in \mathcal{V}$  visited virtual nodes with respect to the sending node X s.t.,  $\bigcup S_j = \mathcal{N} \quad \forall \quad v_j \in \mathcal{V}' \quad and \quad S_i \cap S_j = \emptyset \quad \forall \quad v_i, v_j \in \mathcal{V}' \quad where \quad i \neq j.$ 

**Definition 2.** An invalid tour is a cycle of  $\mathcal{V}' \in \mathcal{V}$  visited virtual nodes with respect to the sending node X s.t.,  $\bigcup S_j \neq \mathcal{N} \quad \forall \quad v_j \in \mathcal{V}' \quad \text{or} \quad S_i \cap S_j \neq \emptyset \quad \forall \quad v_i, v_j \in \mathcal{V}' \quad \text{where} \quad i \neq j.$ 

In the next subsection we present a prize assignment strategy that guarantees that the solution to the TDPCTSP is a valid tour.

## B. TDPCTSP Prize Assignment Strategy

In this subsection, we present a way to assign prizes to virtual nodes that guarantees the selection of a valid tour as the solution to the TDPCTSP instance. Fist and foremost, we form a basis set  $\mathcal{R}$  of virtual nodes from  $\mathcal{V}.\ v_j \in \mathcal{R}$  if and only if  $|S_j| = 1 \quad \forall \quad v_j \in \mathcal{V}$  and  $j \geq 1$ . It is clearly seen that  $|\mathcal{R}| = N$ . We assign to each  $R_l \in \mathcal{R}$  a basis prize  $b_l = \log p_l$  where  $p_l$  is a prime number unique to  $R_l$ . We define the prize  $w_j$  for virtual node  $v_j$  as follows

$$w_j = \begin{cases} 0 \text{ if } j = 0\\ \sum_{l:R_l \in \mathcal{S}_j} b_l \text{ if } j \ge 1 \end{cases}$$
 (5)

The total prize of a valid tour  $w_T$  is therefore

$$w_T = \sum_{l:R_l \in \mathcal{R}} b_l \tag{6}$$

**Theorem 3.** The prize assignment  $w_j = \sum_{l:R_l \in S_j} b_l$  guarantees that the TDPCTSP instance selects mutually disjoint multicast sets.

*Proof.* Suppose the prizes of virtual nodes in the TDPCTSP instance are assigned using Equation 5, we will show that Equation 5 guarantees the selection of mutually disjoint multicast sets in the TDPCTSP solution. In doing this, first and foremost, we prove that all valid tours yield a total prize of  $w_T$ . In addition to this, we also prove that no invalid tour can have a total prize of  $w_T$ .

The intuition behind our proof lies in the Fundamental Theorem of Arithmetic [94], which states that every positive integer can be uniquely represented as the product of prime numbers. From the definition of valid tours in Definition 1, we observe that a valid tour only contains exactly N receivers each present in exactly 1 multicast set. Since each receiver appears exactly once in a valid tour, each receiver is clearly

in  $\mathcal{R}$ . With each  $R_l \in \mathcal{R}$  uniquely assigned a basis prize  $b_l = \log p_l$  where  $p_l$  is a unique prime number, the total prize of the basis  $w_b$  is  $w_b = \log \prod_{l:R_l \in \mathcal{R}} p_l$ . The term  $\prod_{l:R_l \in \mathcal{R}} p_l \in \mathbb{Z}_{>1}$ , hence, as a consequence of the Fundamental Theorem of Arithmetic, it is uniquely prime factorable. It is easy to see that the logarithm of all factors of  $\prod_{l:R_l \in \mathcal{R}} p_l$  yields the basis prizes  $b_l$ . The total prize of the basis  $w_b$ ,  $w_b = \sum_{l:R_l \in \mathcal{R}} b_l = w_T$  where  $w_T$  is the total prize for a valid tour in Equation 6. We have shown that a valid tour always yields a total prize of  $w_T$ , hence the first part of the proof is complete.

The second part of the proof pertains to invalid tours. We provide a proof by way of contradiction. We suppose that there is an invalid tour with total prize  $w_T$ . As seen from the first part of the proof, by assigning logarithms of primes to basis virtual nodes and using the Fundamental Theorem of Arithmetics, a total prize of  $w_T$  is attainable if and only if there are exactly N unique receivers each present in exactly 1 multicast set. Clearly , this is a contradiction since invalid tours either have at least a pair of mutually non exclusive sets or do not contain N distinct receivers.

We have shown that the prize assignment  $w_j = \sum_{l:R_l \in \mathcal{S}_j} b_l$  preserves the selection of mutually disjoint multicast sets in the TDPCTSP instance. The proof is complete.

#### C. Time-Dependent Cost Function

In this subsection we develop a time-dependent cost function for the assignment of edge weights. This is necessary because with mobility, the cost of sending data to a multicast set is not constant over time, but depends on the positions of nodes in the set relative to the sender during the transmission period. To account for the fluctuations in instantaneous data rate, we use the average data rate  $\overline{R_b(t)}$  over a transmission period to estimate the per set data delivery delay.  $R_b(t)$  for node j in set  $S_i$  is expressed as

$$R_b(t) = \frac{M10^{\frac{-\alpha L_j(t)}{10^4}}}{\theta_{S_i}(t)^2 L_i(t)^2} \tag{7}$$

where  $M=\frac{P_tD^2L_{tp}L_{rp}\eta_t\eta_r}{hfN_b}$ ,  $\theta_{S_i}(t)$  is the time-varying divergence angle for set  $S_i$ , and  $L_j(t)$  is the time-varying distance from the receiving node j to the sender X.

In Figures 4a to 4c, we illustrate effect of mobility on time-dependent edge weights. We consider a static transmitter and a mobile receiver moving at a speed of 2 m/s away from the transmitter and initially located 20 m from it (as is the case in Figure 4a). For the sake of analysis we use  $P_t = 60$  mW, g = 8 m,  $N_b = 6$  photons/bit. As the receiver gets farther away from the transmitter,  $\theta$  per the set containing the single receiver decreases (Figure 4b). This is because the farther a node moves from the transmitter, the smaller the  $\theta$  required to meet g becomes (see Subsection III-A). We also observe from Figure 4b that  $\frac{\Delta \theta_{rA}}{\Delta t_{rA}} > \frac{\Delta \theta_{rB}}{\Delta t_{rB}}$  where rA and rB represent regions A and B respectively. In region A,  $\frac{\Delta \theta_{rA}}{\Delta t_{rA}} >> \frac{\Delta \theta_{rB}}{\Delta t_{rB}}$  than that of region B, so  $\theta$  has a greater influence on  $R_b(t)$  compared to the TX-RX distance  $L_j$ . However in region B,  $\frac{\Delta \theta_{rB}}{\Delta t_{rB}}$  is very small, hence,  $R_b(t)$  depends largely on  $L_j$ . This explains the trend in Figure 4c.

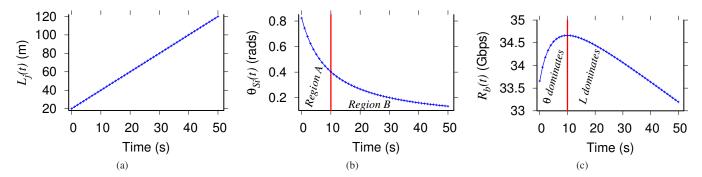


Fig. 4: Illustrating the effect of node mobility on cost. (a) Time-dependent distance between a mobile receiver and a static transmitter, (b) Effect of mobility on divergence angle  $\theta_{S_i}(t)$ , (c) Effect of mobility on instantaneous data rate  $R_b(t)$ .

 $\overline{R_b(t)}$  over a transmission period is

$$\overline{R_b(t)} = \frac{1}{t_f - t_s} \int_{t_s}^{t_f} R_b(t) dt$$
 (8)

with  $t_s$  and  $t_f$  such that

$$P = \int_{t_{-}}^{t_{f}} R_b(t) dt \tag{9}$$

P is the data sent per transmission period. The average cost  $\overline{d}_i$  per set  $S_i$  is

$$d_i = \max_j \left\{ \frac{P}{\overline{R_b}} + d_{al} \right\} \text{ where } 1 \le j \le |S_i|$$
 (10)

where  $\overline{R_b}$  is calculated for each node  $j \in S_i$  using different values of distance  $L_j$  and  $d_{al}$  is the alignment delay.

We use the previously developed set weights (Equations 7 - 10) to come up with an edge weight assignment scheme for the TDPCTSP instance. We formulate our problem on a complete directed graph  $\mathcal{G}=(\mathcal{V},\mathcal{E})$  where virtual nodes  $u\in\mathcal{V}$  and edges  $(u,v)\in\mathcal{E}$ . In performing the translation from M-FSOMP to TDPCTSP, to make the notation easy to follow, we let  $S_u$  correspond to virtual node u. The time-dependent edge weight  $c_{uv}(t)$  for a pair of virtual nodes  $u,v\in\mathcal{V}$  is the cost of sending data to virtual node v (set  $S_v$ ) immediately after sending data to virtual node u (set  $S_u$ ).  $c_{uv}(t)$  is expressed as

$$c_{uv}(t) = \begin{cases} \max_{j} \left\{ \frac{P}{R_b} + d_{al} \right\} \text{ where } 1 \le j \le |S_v| \\ \infty, \quad S_u \cap S_v \ne \emptyset \\ 0, \text{ if } v = X \end{cases}$$
 (11)

The data arrival time at virtual node v in the TDPCTSP instance (i.e. the time  $S_v$  in M-FSOMP receives data) is  $t_v = t_u + c_{uv}$ , where  $t_u$  is the time data arrived at the previous node in the salesman's path (i.e. the time the preceding set  $S_u$  in M-FSOMP receives data). Note that at the origin X,  $t_u = 0$ .

## D. A M-FSOMP to TDPCTSP example

In this subsection, we present a translation of a M-FSOMP scenario into an instance of TDPCTSP. Suppose node X intends to send data to nodes A and B as shown in Figure 5a, the objective is to find the sequence of multicast

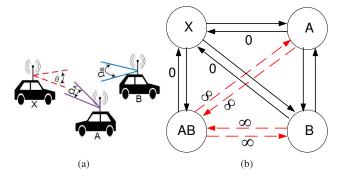


Fig. 5: Conversion from M-FSOMP to TDPCTSP. (a) An instance of M-FSOMP whereby node X intends to send data to nodes A and B with field of views of  $\Omega_A$ ,  $\Omega_B$  respectively, (b) An instance of the TDPCTSP with the objective of finding the shortest tour with respect to X to a subset of virtual nodes subject to prize constraints.

transmissions with minimum total data delivery delay. We assume that nodes X, A and B are mobile. In the M-FSOMP instance, the universe of receiving nodes is  $\mathcal{N} = \{A, B\}$ . With  $N = |\mathcal{N}| = 2$ , we then form K = 3 sets. The collection of sets  $S = \{\{A\}, \{B\}, \{A, B\}\}$ . Each set is then associated with a virtual node. The universe of virtual nodes  $\mathcal{V} = \{X, A, B, AB\}$ . The basis for virtual nodes  $\mathcal{R}$  is then  $\mathcal{R} = \{A, B\}$ . We assign prizes to each member of  $\mathcal{R}$  as described in Subsection IV-B. Virtual nodes A, B and AB are assigned prizes of log 2, log 3 and log 6 respectively. The prize of a valid tour  $w_T$ , which is the sum of the prizes assigned to elements (i.e A and B) in the basis. In this example,  $w_T = \log 2 + \log 3 = \log 6$ . A complete directed graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$  is then formed with  $\mathcal{V} = \{X, A, B, AB\}$ , and edge weights assigned using the cost function in Equation 11. As an example, all edges terminating on X are assigned a 0 weight whiles edges connecting mutually non disjoint virtual nodes (sets) are assigned a weight of  $\infty$  (Figure 5b). The edge weight for a pair of mutually disjoint sets is time dependent.

## E. M-FSOMP 0/1 Integer Linear Program Formulation

We now formulate the M-FSOMP as a 0/1 Integer Linear Program(ILP). The formulation is based on the PCTSP 0/1

ILP and the TDTSP 0/1 ILP presented in [91], [92], [93] and [95], [96] respectively. The problem can now be formulated as follows.

Problem 2. The FSO Multicast Problem with Mobility

$$\sum_{(u,v)\in\mathcal{E}} x_{uv}^z \le 1 \quad \forall \quad z \in \mathcal{Z}$$
 (15)

$$w_T - \epsilon \le \sum_{u \in \mathcal{V}} w_u y_u \le w_T + \epsilon \tag{16}$$

$$\left(\sum_{(u,v)\in\mathcal{E}} x_{uv}^{z_b} \sum_{(u,v)\in\mathcal{E}} x_{uv}^{z_a}\right) \\
\left(\left(z_b - z_a\right) s_w - d_{al} - \sum_{(u,v)\in\mathcal{E}} c_{uv}^{z_a} x_{uv}^{z_a}\right) \ge 0 \\
\forall \quad z_a, z_b \in \mathcal{Z} \quad s.t. \quad z_b > z_a \tag{17}$$

where  $y_u \in \{0,1\}; x_{uv}^z \in \{0,1\};$ 

$$u, v \in \mathcal{V}; (u, v) \in \mathcal{E}; z \in \mathcal{Z}$$
 (18)

In the objective (Equation 12), the time-dependent weight  $c_{uv}^z$  of edge (u,v) is obtained using a discretized version of Equation 11.  $c_{uv}^z$  is the average cost on edge (u,v) when data is sent at any time within slot z to multicast set (virtual node) v, immediately after a transmission to set u. To derive  $c_{uv}^z$ , it is necessary to obtain an upper bound  $t_{up}$  on the total time required to multicast data to all receivers. Since the total multicast cost for the optimum sequence of transmissions is upper bounded by the cost of any valid sequence of transmissions,  $t_{up}$  is basically the cost of a valid sequence (e.g. a sequence of unicast sets or a single broadcast set). With  $t_u$  for the first transmission  $t_{u1}$  in the sequence known (i.e. 0 s),  $Z = |\mathcal{Z}|$  non-overlapping time slots each of width  $s_w$  are created from the  $t_{u1}$  to  $t_{up}$  interval with each time slot  $t_{u1}$ 

 $x_{uv}^z$  is 1 if edge (u,v) in time slot z is selected to be in the optimum tour and 0 if otherwise.  $y_u$  is 1 if virtual node u is selected to be in the optimum tour and 0 if otherwise. Since the prize collecting constraint (Equation 16) guarantees that all receivers in the M-FSOMP get the broadcast data, the penalty  $h_l$  incurred if virtual node l is not visited is set to 0. The constraints in Equation 13- 14 guarantee that any virtual node in the optimum tour has exactly one incoming and one outgoing edge. Constraint Equation 15 ensures that at most one edge is chosen per time slot. In other words, at most one transmission to a multicast set can begin in each time slot. The prize collecting constraint is given in Equation 16. Taking into account that  $w_T$  might be irrational because it is the sum of

logarithms, we subject the total prize collected to a lower and upper bound of  $w_T$ .

In Equation 17, we introduce the alignment constraints. For a pair of slots  $z_a$  and  $z_b$  such that slot  $z_a$  precedes  $z_b$ , we formulate constraints that ensure that the commencement of a transmission in a selected slot only occurs at least  $d_{al}$  seconds after the end of the preceding transmission. We observe that since  $z_b > z_a$ , there are  $\frac{Z(Z-1)}{2}$  such constraints with each having  $\mathcal{O}(|\mathcal{V}|^2|)$  terms.

#### V. COMPARISON BETWEEN S-FSOMP AND M-FSOMP

We present a comparison between the solutions developed to address multicast in static and mobile scenarios. Using the same procedure in Subsection IV-A, it is easy to see that S-FSOMP can be translated into an instance of PCTSP. We briefly present an alternative to the MWSC formulation of S-FSOMP.

## Problem 3. S-FSOMP as a PCTSP

minimize 
$$\left(\sum_{u \in \mathcal{V}} \sum_{v \in \mathcal{V} \setminus \{u\}} (c_{uv} + d_{al}) x_{uv} + \sum_{u \in \mathcal{V}} h_u (1 - y_u)\right) - d_{al}$$
(19)

subject to 
$$\sum_{v \in \mathcal{V} \setminus \{u\}} x_{uv} - y_u = 0 \quad \forall \quad u \in \mathcal{V}$$
 (20)

$$\sum_{u \in \mathcal{V} \setminus \{v\}} x_{uv} - y_v = 0 \quad \forall \quad v \in \mathcal{V}$$
 (21)

$$w_0 - \epsilon \le \sum_{u \in \mathcal{V}} w_u y_u \le w_0 + \epsilon \tag{22}$$

where 
$$y_u \in \{0, 1\}; x_{uv} \in \{0, 1\}$$
  
 $u, v \in \mathcal{V}; (u, v) \in \mathcal{E}$  (23)

The symbols, constraints, and variables are identical to those in Problem 2, with the only difference being the exclusion of time-dependent variables and constraints. Note that in the objective(Equation 19) of S-FSOMP, the alignment delay  $d_{al}$  is factored into the cost of a multicast set. Bearing in mind that a sequence of Q consecutive multicast transmissions incurs Q-1 alignment delays, we subtract one  $d_{al}$  in the objective. S-FSOMP in Problem 3 contains  $\mathcal{O}(|\mathcal{V}|^2)$  variables and  $\mathcal{O}(|\mathcal{V}|)$  constraints whiles the equivalent formulation in Problem 1 uses  $\mathcal{O}(|\mathcal{V}|^2)$  variables and  $\mathcal{O}(N)$  constraints. With the TDPCTSP formulation of M-FSOMP, the total number of variables involved is  $\mathcal{O}(|\mathcal{V}|^2|\mathcal{Z}|)$ , with  $\mathcal{O}(Z^2)$  constraints assuming  $|\mathcal{Z}| \gg |\mathcal{V}|$ . Clearly, TDPCTSP can be used to solve S-FSOMP, however due to its larger number of variables and constraints, it is more computationally complex to solve relative to using either the MWSC or PCTSP formulations in static scenarios. Due to the M-FSOMP being NP-hard, in the next few subsections, we provide heuristics to solve the mobile multicast problem based on two main approaches: a mobile time dependent greedy heuristic, and mobile heuristics based on static approaches.

# A. Mobile Time-Dependent Greedy Heuristic

The time-dependent greedy heuristic (M-TDH, Algorithm 3) described in this subsection is fundamentally similar to Algo-

**Algorithm 3:** Time-Dependent Greedy Heuristic (M-TDH)

```
Input: A universe S = \{S_1, S_2, ..., S_K\} of K = N^2 - N + 1
     Output: An ordered subcollection of sets S'' that covers the
                   universe of \mathcal{U} = \{n_1, n_2, \dots, n_N\} of N nodes
 1 for S_j \in \mathcal{S} s.t. j \leftarrow 1 to K do
     compute w_j using Equation 5
 3 for n_x \in \mathcal{U} s.t. x \leftarrow 1 to N do
     compute w_T using Equation 6
 5 w_R \leftarrow 0
 \mathbf{6} \ \mathcal{S}'' \leftarrow \emptyset
 7 \mathcal{U}'' \leftarrow \emptyset
 8 At initial start time t_s = t_0, for S_j \in \mathcal{S}' s.t. j \leftarrow 1 to K do
     compute d_j using Equation 10
10 j^* = \min \frac{d_j}{|S_j|}
11 \mathcal{S}'' \leftarrow \check{S}_{j^*}
12 \mathcal{U}'' \leftarrow \mathring{S_{j^*}}
13 t_f \leftarrow t_s + d_{j*}
14 w_R \leftarrow w_{j^*}
15 while w_R \neq w_T do
           for S_i \in \mathcal{S} do
                 update d_j at t_s = t_f using Equation 10
17
                 \frac{d_j}{|S_j|} \leftarrow \frac{d_j}{|S_j - \mathcal{U}''|}
18
           j^* = \min \frac{d_j}{|S_i|}
19
           \mathcal{S}'' \leftarrow \mathcal{S}'' \bigcup S_{i^*}
20
           \mathcal{U}'' \leftarrow \mathcal{U}'' \bigcup \vec{S}_{j^*}
21
           t_f \leftarrow t_s + \bar{d}_{j^*}
22
23
           w_R \leftarrow w_R + w_{i^*}
```

rithm 2 for the static case, with the main difference being the incorporation of time-dependent set weights. Algorithm 3 takes as input the universe of K sets and yields an ordered subcollection of sets S''. In lines 1 to 2, the prize associated with each set(virtual node) is computed. The total prize of covering each node is computed in lines 3 to 4. A running total prize  $w_R$ , and the current cover are initialized in lines 5 to 7. At the initial start time for a session, the time dependent weights for each set is computed (lines 8 to 9). The most cost effective set is chosen and placed in the cover, the finish time  $t_f$  of the first transmission is initialized, and the running total prize updated (lines 10 to 14). In lines 15 to 23, whiles the total prize has not been met, the cost effectiveness of each set is updated and the most effective set placed in the cover. This process repeats itself till the total prize is met. Note that, similar to Theorem 2, this algorithm yields mutually disjoint sets.

#### B. Mobile Heuristics Based on Static Approaches

In our previous works [9], [4], [10], we introduced static multiple unicast (S-MU), the static optimal set cover solution (S-SC), the static local optimum heuristic (S-HEU), and the standard approximation algorithm to the set cover solution (S-AP) to optimize multicast in static and emulated static conditions in mobile networks. In this subsection, we describe a greedy approach to mobile multicast using solutions obtained from static schemes. As established in Theorem 1, Theorem 2,

Algorithm 4: Mobile Multicast Based on Static Set Selection

```
Input: A subcollection of sets S' based on the output of either
                    S-MU, S-SC, S-HEU, S-AP
     Output: An ordered subcollection of sets S''
 2~\mathcal{U}' \leftarrow \emptyset
 3 At initial start time t_s = t_0, for S_j \in \mathcal{S}' s.t. j \leftarrow 1 to |\mathcal{S}'| do
       compute d_j using Equation 10
 5 \ j^* = \min \frac{d_j}{|S_i|}
 8 t_f \leftarrow t_s + d_{j^*}
9 while \mathcal{S}'' - \mathcal{S}' \neq \mathcal{S}' - \mathcal{S}'' do
             for S_j \in \mathcal{S}' do
10
                \begin{array}{c} \text{update } d_j \text{ at } t_s = t_f \text{ using Equation 10} \\ \frac{d_j}{|S_j|} \leftarrow \frac{d_j}{|S_j - \mathcal{U}'|} \end{array} 
11
12
             j^* = \min_{|S_i|} \frac{d_j}{|S_i|}
13
             \mathcal{S}'' \leftarrow \mathcal{S}'' \bigcup_{j=1}^{j} S_{j}
14
             \mathcal{U}'' \leftarrow \mathcal{U}'' \bigcup \vec{S}_j
15
              t_f \leftarrow t_s + \bar{d}_{i^*}
16
```

by the definition of multiple unicast (Subsection III-B) and the operation of the heuristic(Subsection 2), S-SC, S-AP, S-MU and S-HEU all yield mutually disjoint multicast sets. The algorithm (Algorithm 4) takes as input the sets computed by the static schemes and yields an ordered collection of these sets. In lines 3 to 7, the most cost effective set at the start of the multicast session is chosen and placed into the new cover. The time the transmission to this set is complete is computed in line 8. In lines 9 to 16, the cost effectiveness of each set is updated and the most cost effective (least cost per uncovered elements) chosen. Note that the input sets to the algorithm are mutually disjoint. This process of iterative picking sets continues till a complete ordered collection of sets is obtained.

#### VI. PERFORMANCE EVALUATION

In this section, we analyze results for various mobile multicast schemes: multiple unicast (S-MU) which greedily performs N unicasts, our proposed time-dependent heuristic (Algorithm 3) and the optimal set cover solution with greedy modifications (S-SC, III-D and Algorithm 4). We do not present results for S-AP and S-HEU since they were very identical to S-SC. The reason being that S-SC, S-AP and S-HEU are all inherently based on static set selections and as such yield similar results when applied to a mobile scenario. For a performance comparison of S-SC, S-AP and S-HEU in static and emulated mobile networks, we refer the interested reader to our previous work in [10].

# A. Simulation Setup

For the evaluation of the various multicast schemes, we simulate an optical 5G backhaul network whereby a static node (e.g. a 5G macro-cell base station on the roof top of a building) sends data to mobile nodes (e.g mobile 5G micro-cell

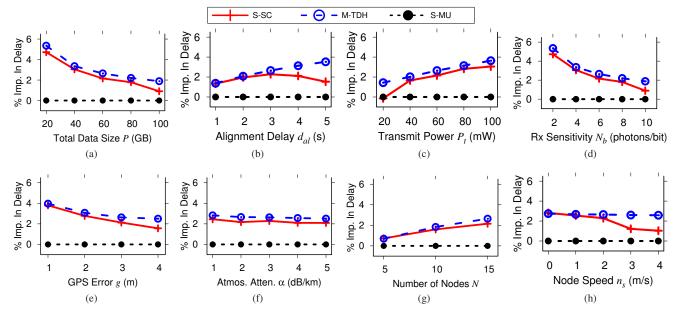


Fig. 6: Percentage improvement in delay w.r.t. S-MU for different multicast approaches versus various network parameters. (a) Effect of P on delay for P=20-100 GB, (b) Effect of  $d_{al}$  on delay for  $d_{al}$ =1-5 s, (c) Effect of P on delay for P=20-100 mW, (d) Effect of P0 on delay for P0 on delay for P0 on delay for P1-20-100 mW, (g) Effect of P1 on delay for P2-10 photons/bit, (e) Effect of P3 on delay for P3-1-4 m, (f) Effect of P4 on delay for P3-1-5 dB/km, (g) Effect of P5 on delay for P5-15, (h) Effect of P6 on delay for P8-1-4 m/s.

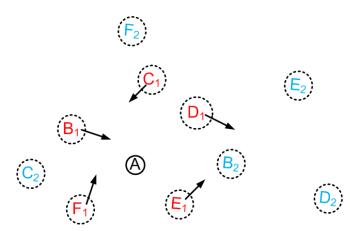


Fig. 7: The mobility model used in the simulations. A static 5G macro-cell BS mounted on a roof top (node A) sends data to multiple 5G micro-cell BSs on trains (Nodes B to F). Nodes B to F at time  $t_1$  choose random destinations where they move towards and arrive at time  $t_2$  (denoted by locations  $B_2 ldots F_2$ ).

base stations on trains). The mobile nodes randomly choose a destination, and move linearly towards it as illustrated in Figure 7. Mobile nodes move with speeds of 0 - 4 m/s. A single message (several GBs) was created at the static node and relayed to all mobile receivers. The mobile receivers were simulated to move away from the static node. Each receiving node is between 100 m and 200m from the sender at the commencement of the multicast session. We use a default of 10 mobile receiving base stations which translates to a base station density of node density of about 250 BSs/km<sup>2</sup>. Our simulation environment was a Java based simulator which we built. In our work, we address issues that might arise when

nodes enter or exit the network during an ongoing data transmission session to recipients. Assuming a new node comes into the network in the middle of a session, transmissions are not made to that new node. The new node becomes part of a new session when the current session is complete. In the case of a node leaving the network during a session, if that node has not yet received multicast data, the transmitter aborts data transfer to the node that has left.

We evaluate the performance of the solutions for this scenario using total delay and throughput as metrics. Each data point is the result of an average of 100 random runs. The parameters we use for the analysis are data size P, alignment delay  $d_{al}$ , receiver sensitivity  $N_b$ , localization error g, FSO transmit power  $P_t$ , number of mobile nodes N, atmospheric attenuation  $\alpha$ , and node speed  $v_s$ . The default values (and ranges) used are: P=60 GB (20-100 GB),  $d_{al}$ =3 s (1-5 s),  $N_b$ =6 photons/bit (2-10 photons/bit), g = 3 m (1-4m),  $P_t$ =60 mW (20-100 mW), N=15 (5-15),  $v_s$ =2 m/s (0-4 m/s),  $\alpha$ =3 dB/km (1-5 dB/km). In addition, we used a wavelength of 1550 nm, and a receiver diameter D=12 mm.

## B. Delay and Average Throughput

The delay metric quantifies the time required to relay data from the static node to all mobile receivers. We present delay results (Figures 6a to 6h) as percentage improvements over the S-MU baseline. We define average throughput to be aggregate throughput (total data transferred/total time taken) divided by the number of nodes. The effect of various parameters on average throughput is shown in Figure 8 again using percentage improvements over the S-MU baseline.

In addition to these figures, we make available in Table II raw data of the actual S-MU delay results which were used in

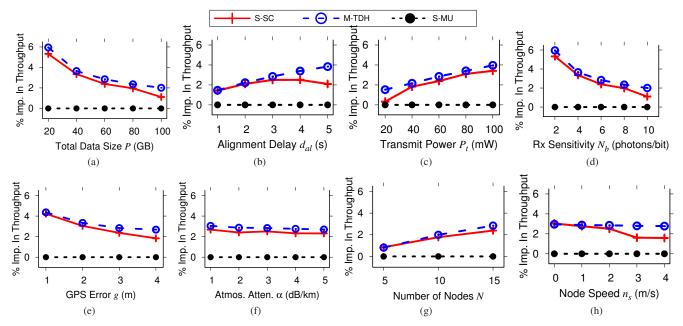


Fig. 8: Percentage improvement in throughput w.r.t. S-MU for different multicast approaches versus various network parameters. (a) Effect of P on throughput for P=20-100 GB, (b) Effect of  $d_{al}$  on throughput for  $d_{al}=1-5$  s, (c) Effect of P on throughput for  $P_t=20-100$  mW, (d) Effect of  $P_t=20-100$  mW, (d) Effect of  $P_t=20-100$  mW, (e) Effect of  $P_t=20-100$  mW, (g) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (g) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (g) Effect of  $P_t=20-100$  mV, (h) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (g) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (g) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20-100$  mV, (e) Effect of  $P_t=20-100$  mV, (f) Effect of  $P_t=20$ 

		P for Figure:	s oa and 8a			
Metric	20 GB	40 GB	60 GB	80 GB	100 GB	
Delay (s)	53.48	64.21	54.21 75.28		97.95	
TPut (Gbps)	2.99	4.98	6.38	7.40	8.17	
		d <sub>al</sub> for Figure	es 6b and 8b			
Metric	1 s	2 s	3 s	4 s	5 s	
Delay (s)	46,67	60,96	75.28	89.60	103.92	
TPut (Gbps)	10.29	7.87	6.38	5.36	4.62	
		$P_t$ for Figure	o 6a and 8a			
Metric	20 mW	40 mW	60 mW	80 mW	100 mW	
Delay (s)	145.91	92.27	75.28	66.97	62.06	
TPut (Gbps)	3.29	5.20	6.38	7.17	7.73	
11 ut (Gops)	3.29	3.20	0.56	7.17	1.13	
		$N_b$ for Figure	es 6d and 8d			
Metric	2 ph/bit	4 ph/bit	6 ph/bit	8 ph/bit	10 ph/bit	
Delay (s)	53.42	64.20	75.28	86.54	97.98	
TPut (Gbps)	8.98	7.48	6.38	5.55	4.90	
Metric	1 s	g for Figures	3 s	4	S	
Delay (s)	46.50	57.05 75.28		101.87		
TPut (Gbps)	10.32	8.41	6.38	4.71		
(1-)		- f F			-	
Metric	1 dB/km		s 6f and 8f	4 dR/km	5 dB/km	
Metric	1 dB/km	2 dB/km	3 dB/km	4 dB/km		
Delay (s)	72.14	2 dB/km 73.60	3 dB/km 75.28	77.09	79.07	
		2 dB/km 73.60 6.52	3 dB/km 75.28 6.38			
Delay (s) TPut (Gbps)	72.14 6.65	2 dB/km 73.60 6.52 N for Figure:	3 dB/km 75.28 6.38 s 6g and 8g	77.09 6.27	79.07 6.07	
Delay (s) TPut (Gbps)	72.14 6.65	2 dB/km 73.60 6.52 N for Figure	3 dB/km 75.28 6.38 s 6g and 8g	77.09 6.27	79.07 6.07	
Delay (s) TPut (Gbps) Metric Delay (s)	72.14 6.65	2 dB/km 73.60 6.52 N for Figure:	3 dB/km 75.28 6.38 s 6g and 8g 10	77.09 6.27	79.07 6.07	
Delay (s) TPut (Gbps)	72.14 6.65	2 dB/km 73.60 6.52 N for Figure:	3 dB/km 75.28 6.38 s 6g and 8g	77.09 6.27	79.07 6.07	
Delay (s) TPut (Gbps) Metric Delay (s)	72.14 6.65	2 dB/km 73.60 6.52 N for Figure:	3 dB/km 75.28 6.38 8 6g and 8g 10 8.84 83	77.09 6.27	79.07 6.07	
Delay (s) TPut (Gbps)  Metric Delay (s) TPut (Gbps)  Metric	72.14 6.65 5 22.76 21.09	2 dB/km 73.60 6.52 N for Figure: 1 48 9.	3 dB/km 75.28 6.38 6 6g and 8g 10 8.84 8.83 8 6h and 8h 2 m/s	77.09 6.27 1 75 6.	79.07 6.07 5 .28 38	
Delay (s) TPut (Gbps)  Metric Delay (s) TPut (Gbps)	72.14 6.65 5 22.76 21.09	$2 \text{ dB/km}$ $73.60$ $6.52$ N for Figure:  48 9. $v_s$ for Figure	3 dB/km 75.28 6.38 s 6g and 8g 0 .84 .83	77.09 6.27 1 75 6.	6.07 5 .28 38	

TABLE II: S-MU delay and throughput data used to compute the percentage improvements for the other schemes in Figures 6a to 8h.

the creation of Figures 6a to 6h. That being said, results in this section would be interpreted by jointly considering Figures 6a to 8h and Table II.

Before we explain the results in detail, we first would like to provide an intuition as to why the performance improvements are generally less than 6%. With 15 nodes, a GPS accuracy

g of 3m, and with each receiver at least 100 m from the sender at the start of the multicast session, the minimum divergence angle  $\theta$  per node is about 0.06 rad. Since the transmitter is steerable, it has a  $2\pi$  transmission footprint. Assuming that nodes are evenly distributed within this footprint, the angular azimuthal spatial separation between an ordered (anti)clockwise pair of receivers  $|\phi_{i+1} - \phi_i|$  is approximately 0.42 rad. With  $|\phi_{i+1} - \phi_i| >> \theta$ , and given the fact that  $R_b \propto \theta^{-2}$ , it is easy to see why algorithms would generally tend to yield multiple unicast set selections. In other words, node density plays a critical role in when receivers are grouped into sets.

In all our delay and throughput results, both M-TDH and S-SC perform better than S-MU. M-TDH has the best improvements in delay and throughput primarily because it is an inherently mobile multicast scheme. S-SC and S-MU on the other hand are schemes designed for static scenarios, but enhanced through a greedy ordering of selected sets to suit mobile scenarios. In Figures 6a and 8a, as data size Pincreases, delay increases and throughput decreases across all schemes. This is because the bigger the P, the longer the per set data transmission delay. This directly translates into a longer total delay (smaller throughput) per multicast session. We also observe that there is a decline in percentage improvements in delay and throughput as P grows larger. When P is small,  $\frac{P}{\overline{R}_b} << d_{al}$  for sets  $S_i$  with  $|S_i| > 1$  and a dense intra angular separation of nodes. These sets tend to be chosen in the cover. For such sets,  $|S_i| > 1$ , hence there are fewer realignments relative to S-MU which suffers from N-1realignments. This explains why performance improvements are higher at lower data sizes. At larger data sizes,  $\frac{P}{R_i}$  and  $d_{al}$ 

are of similar orders of magnitude, resulting in a selection of mostly unicast sets.

The effect of alignment delay  $d_{al}$  on delay and throughput are evaluated in Figures 6b and 8b respectively. As expected, for the three schemes, an increase in  $d_{al}$  leads to a rise in total delay and a decline in throughput. This is due to the fact that the greater  $d_{al}$ , the longer it takes the last bit to reach the farthest recipient in the last set in the ordered collection of transmissions. As was the case in the relationship between data size P and the evaluated metrics, for large values of  $d_{al}$ ,  $\frac{P}{R_b} << d_{al}$ , and sets with multiple constituent nodes are typically chosen. When  $d_{al}$  is large,  $\frac{P}{R_b}$  and  $d_{al}$  are comparable, with unicasting being the likeliest outcome in such scenarios. M-TDH has the best improvement in delay and throughput because it factors in time-dependent set costs when greedily picking up sets to construct the cover.

A characterization of the impact transmit power  $P_t$  has on delay and throughput is presented in Figures 6c and 8c. There is a decrease in total delay (increase in throughput) for S-MU, S-SC and M-TDH as  $P_t$  increases. This is fairly intuitive since the per set transmission delay reduces with increasing  $P_t$ . The trend in Figures 6c and 8c can be explained by observing that sets which have sizes greater than 1 and have a dense spatial topology of nodes within it have the tendency to be selected as  $P_t$  grows. A reduction on the number of realignments over S-MU accounts for the rise in the improvements in delay and throughput of M-TDH and S-SC. With respect to transmit power, receiver sensitivity  $N_b$  has a reverse effect on delay and throughput. This is because, they are both scalars in Equation 1, and affect  $R_b$  in inverse ways. The reasons behind the trends in Figures 6c and 8c can be extended to support the trends in Figures 6d, and 8d.

We accounted for potential localization errors via the GPS accuracy parameter g. When g is known, the minimum divergence angle per set  $\theta$  can be set in such a manner that the boundaries of the transmitted FSO beam are tangential to the circumference of the localization error region around nodes at the extreme edges of the set. Clearly for all schemes, an increase in g yields to a surge in delay and a reduction in throughput. The reason for this is, as g increases  $\theta$  for all sets increases, leading to a reduction in  $R_b$  and an increase in delay per set. Subsequently, the aggregate delay increases. M-TDH has a better improvement in delay and throughput over S-SC, with both schemes offering superior performance relative to S-MU in Figures  $\theta$ e and  $\theta$ e.

In discussing the effect of atmospheric attenuation  $\alpha$  on delay and throughput, we consider the relationship between  $\alpha$  and  $R_b$  in Equation 1.  $R_b$  depends on  $\alpha$  exponentially. The 1-5 dB/km attenuation factors are typical to clear sky.  $\alpha$  in that range does not significantly affect  $R_b$ . This explains the slight improvements in delay and throughput as seen in Figures 6f and 8f.

A network with a large number of receivers, incurs a larger total delay than a smaller one. In the case of S-MU, the reason is quite obvious, more sets (realignments) are required to reach all receivers. In the case of schemes in which the set size is not limited to a single node, generally as N increases, either the

number of sets, the divergence angle per set, or both increase. This leads to a growth in delay and a fall in throughput. In relation to Figures 6g and 8g, an increase in N means greater node density. Greater node density further implies a larger pool of sets to pick the collection of consecutive transmissions from. As N grows, there is the tendency to select non unicast sets. This explains why at N=5, there is just an approximately 0.8% improvement in delay and throughput for M-TDH as compared to a 2.8% improvement when N=15.

In discussing the effect of node speed  $v_s$  on delay and throughput, we would leverage on concepts from Subsection IV-C. Using the results from Table II, there is a slight increase in delay (decrease in throughput) as  $v_s$  increases from 0 to 4 m/s. Figure 4 shows a dependence of  $R_b(t)$  for node j in set  $S_i$  on both the set's divergence  $\theta_{S_i}(t)$  and its distance  $L_j(t)$  from the sender. The closer a node is to the transmitter, the larger the  $\theta_{S_i}$  and smaller the  $L_j$  is. Nodes farther away have a smaller  $\theta_{S_i}$  but a larger  $L_j$ . With these dynamics, determining which of the two parameters has a larger influence on  $R_b(t)$  can sometimes be intricate since  $R_b(t)$  depends inversely with the square of both terms (see Equation 7).

#### VII. CONCLUSION

In this paper, we presented a compendium of multicast techniques which can be used for fixed and mobile optical wireless backhaul in 5G network. We showed that the optimal multicast problem can be translated time-dependent prize collecting traveling salesman problem. In formulating the optimal multicast problem with mobility, we developed a prize assignment strategy and proved that such a strategy guaranteed the selection of a valid tour of mutually non-disjoint multicast sets. With the problem known to be NP-hard, we provided and evaluated several potential heuristics for multicast in mobile scenarios.

## REFERENCES

- [1] X. Ge, S. Tu, G. Mao, C. X. Wang, and T. Han, "5g ultra-dense cellular networks," *IEEE Wireless Communications*, vol. 23, no. 1, pp. 72–79, February 2016.
- [2] N. Hamedazimi, Z. Qazi, H. Gupta, V. Sekar, S. R. Das, J. P. Longtin, H. Shah, and A. Tanwer, "FireFly: A Reconfigurable Wireless Data Center Fabric Using Free-space Optics," in *Proceedings of the 2014 ACM Conference on SIGCOMM*, ser. SIGCOMM '14. New York, NY, USA: ACM, 2014, pp. 319–330. [Online]. Available: http://doi.acm.org/10.1145/2619239.2626328
- [3] J. Bao, D. Dong, B. Zhao, Z. Luo, C. Wu, and Z. Gong, "FlyCast: Free-Space Optics Accelerating Multicast Communications in Physical Layer," in *Proceedings of the 2015 ACM Conference on Special Interest Group on Data Communication*, ser. SIGCOMM '15. New York, NY, USA: ACM, 2015, pp. 97–98. [Online]. Available: http://doi.acm.org/10.1145/2785956.2790002
- [4] M. Atakora and H. Chenji, "Overcoming alignment delay in RF+FSO networks (invited paper)," in 2017 IEEE IWCMC Wireless Optical Networks Syposium (IWCMC 2017 WON Syposium), ser. IWCMC 2017, Valencia, Spain, Jun. 2017.
- [5] "Koruza." [Online]. Available: http://koruza.net/
- [6] H. A. Willebrand and B. S. Ghuman, "Fiber optics without fiber," *IEEE Spectrum*, vol. 38, no. 8, pp. 40–45, Aug. 2001.
- [7] D. W. Young, H. H. Hurt, J. E. Sluz, and J. C. Juarez, "Development and Demonstration of Laser Communications Systems," *John Hopkins APL Technical Digest*, vol. 33, no. 2, pp. 122–138, Sep. 2015.
- [8] A. K. Majumdar, Advanced Free Space Optics (FSO), ser. Springer Series in Optical Sciences. New York, NY: Springer New York, 2015, vol. 186. [Online]. Available: http://link.springer.com/10.1007/ 978-1-4939-0918-6

- [9] M. Atakora and H. Chenji, "Optimal multicasting in hybrid RF/FSO DTNs," in 2016 IEEE Global Communications Conference: Optical Networks and Systems (Globecom2016 ONS), ser. GLOBECOM '16, Washington, USA, Dec. 2016.
- [10] —, "Multicast techniques for hybrid rf/fso dtns," IEEE/OSA Journal of Optical Communications and Networking, vol. 9, no. 11, pp. 1051– 1061, Nov 2017.
- [11] Small Cell Forum, "Small cells whats the big idea?" Tech. Rep., Feb. 2012.
- [12] Qualcomm Research, "Enabling Hyper-Dense Small Cell deployments with UltraSON," Tech. Rep., Feb. 2014.
- [13] N. Bhushan, J. Li, D. Malladi, R. Gilmore, D. Brenner, A. Damnjanovic, R. T. Sukhavasi, C. Patel, and S. Geirhofer, "Network densification: the dominant theme for wireless evolution into 5g," *IEEE Communications Magazine*, vol. 52, no. 2, pp. 82–89, February 2014.
- [14] S. Chia, M. Gasparroni, and P. Brick, "The next challenge for cellular networks: backhaul," *IEEE Microwave Magazine*, vol. 10, no. 5, pp. 54–66, August 2009.
- [15] S. Hur, T. Kim, D. J. Love, J. V. Krogmeier, T. A. Thomas, and A. Ghosh, "Millimeter wave beamforming for wireless backhaul and access in small cell networks," *IEEE Transactions on Communications*, vol. 61, no. 10, pp. 4391–4403, October 2013.
- [16] Z. Zhang, X. Wang, K. Long, A. V. Vasilakos, and L. Hanzo, "Large-scale mimo-based wireless backhaul in 5g networks," *IEEE Wireless Communications*, vol. 22, no. 5, pp. 58–66, October 2015.
- [17] C. Dehos, J. L. Gonzlez, A. D. Domenico, D. Ktnas, and L. Dussopt, "Millimeter-wave access and backhauling: the solution to the exponential data traffic increase in 5g mobile communications systems?" *IEEE Communications Magazine*, vol. 52, no. 9, pp. 88–95, September 2014.
- [18] X. Ge, H. Cheng, M. Guizani, and T. Han, "5g wireless backhaul networks: challenges and research advances," *IEEE Network*, vol. 28, no. 6, pp. 6–11, Nov 2014.
- [19] R. Taori and A. Sridharan, "Point-to-multipoint in-band mmwave back-haul for 5g networks," *IEEE Communications Magazine*, vol. 53, no. 1, pp. 195–201, January 2015.
- [20] Z. Pi, J. Choi, and R. Heath, "Millimeter-wave gigabit broadband evolution toward 5g: fixed access and backhaul," *IEEE Communications Magazine*, vol. 54, no. 4, pp. 138–144, April 2016.
- [21] A. Douik, H. Dahrouj, T. Y. Al-Naffouri, and M. S. Alouini, "Hybrid Radio/Free-Space Optical Design for Next Generation Backhaul Systems," *IEEE Transactions on Communications*, vol. 64, no. 6, pp. 2563– 2577, Jun. 2016.
- [22] H. Dahrouj, A. Douik, F. Rayal, T. Y. Al-Naffouri, and M. S. Alouini, "Cost-effective hybrid RF/FSO backhaul solution for next generation wireless systems," *IEEE Wireless Communications*, vol. 22, no. 5, pp. 98–104, Oct. 2015.
- [23] A. Douik, H. Dahrouj, T. Y. Al-Naffouri, and M. S. Alouini, "Cost-effective backhaul design using hybrid radio/free-space optical technology," in 2015 IEEE International Conference on Communication Workshop (ICCW), ser. ICCW '15, Jun. 2015, pp. 7–12.
- [24] Facebook, "Connectivity Lab," Jul. 2017. [Online]. Available: https://info.internet.org/en/story/connectivity-lab/
- [25] T. Peyronel, K. J. Quirk, S. C. Wang, and T. G. Tiecke, "Luminescent detector for free-space optical communication," *Optica*, vol. 3, no. 7, pp. 787–792, Jul 2016. [Online]. Available: http://www.osapublishing. org/optica/abstract.cfm?URI=optica-3-7-787
- [26] A. G. Talmor, H. Harding, and C.-C. Chen, "Two-axis gimbal for air-to-air and air-to-ground laser communications," *Proc. SPIE*, vol. 9739, pp. 97390G–97390G–7, 2016. [Online]. Available: http://dx.doi. org/10.1117/12.2218097
- [27] S. Guo, M. Guo, V. C. M. Leung, S. Yu, and Y. Xiang, "On the multicast lifetime of wanets with multibeam antennas: Formulation, algorithms, and analysis," *IEEE Transactions on Computers*, vol. 63, no. 8, pp. 1988–2001, Aug 2014.
- [28] J. E. Wieselthier, G. D. Nguyen, and A. Ephremides, "The impact of directional antennas on energy-aware, session-based multicasting in ad hoc wireless networks," in *Military Communications Conference*, 2001. MILCOM 2001. Communications for Network-Centric Operations: Creating the Information Force. IEEE, ser. MILCOM '01, vol. 2, 2001, pp. 947–951 vol. 2.
- [29] —, "Energy-aware wireless networking with directional antennas: the case of session-based broadcasting and multicasting," *IEEE Transactions* on *Mobile Computing*, vol. 1, no. 3, pp. 176–191, Jul 2002.
- [30] —, "Energy-limited wireless networking with directional antennas: the case of session-based multicasting," in INFOCOM 2002. Twenty-First Annual Joint Conference of the IEEE Computer and Communica-

- tions Societies. Proceedings. IEEE, ser. INFOCOM '02, vol. 1, 2002, pp. 190–199 vol.1.
- [31] S. Guo, M. Guo, and V. Leung, "Exploring the multicast lifetime capacity of wanets with directional multibeam antennas," in *IEEE INFOCOM 2009*, April 2009, pp. 2686–2690.
- [32] R. Vaishampayan, J. J. Garcia-Luna-Aceves, and K. Obraczka, "Efficient multicasting in multi-hop ad hoc networks using directional antennas," in *IEEE International Conference on Mobile Adhoc and Sensor Systems Conference*, 2005., Nov 2005, pp. 9 pp.–664.
- [33] C.-C. Shen, Z. Huang, and C. Jaikaeo, "Directional broadcast for mobile ad hoc networks with percolation theory," *IEEE Transactions on Mobile Computing*, vol. 5, no. 4, pp. 317–332, April 2006.
- [34] A. Nasipuri, J. Mandava, H. Manchala, and R. E. Hiromoto, "On-demand routing using directional antennas in mobile ad hoc networks," in *Proceedings Ninth International Conference on Computer Communications and Networks (Cat.No.00EX440)*, 2000, pp. 535–541.
- [35] Y. T. Hou, Y. Shi, H. D. Sherali, and J. E. Wieselthier, "Online lifetime-centric multicast routing for ad hoc networks with directional antennas," in *INFOCOM 2005. 24th Annual Joint Conference of the IEEE Computer and Communications Societies. Proceedings IEEE*, ser. INFOCOM '05, vol. 1, March 2005, pp. 761–772 vol. 1.
- [36] —, "Multicast communications in ad hoc networks using directional antennas: A lifetime-centric approach," *IEEE Transactions on Vehicular Technology*, vol. 56, no. 3, pp. 1333–1344, May 2007.
- [37] S. Guo, O. Yang, and V. Leung, "Approximation algorithms for longest-lived directional multicast communications in wanets," in Proceedings of the 8th ACM International Symposium on Mobile Ad Hoc Networking and Computing, ser. MobiHoc '07. New York, NY, USA: ACM, 2007, pp. 190–198. [Online]. Available: http://doi.acm. org/10.1145/1288107.1288133
- [38] S. Guo, V. Leung, and X. Jiang, "Distributed approximation algorithms for longest-lived multicast in wanets with directional antennas," *IEEE Transactions on Wireless Communications*, vol. 9, no. 7, pp. 2227–2237, July 2010.
- [39] S. Guo, V. C. M. Leung, and O. W. W. Yang, "Wsnp1-7: Distributed multicast algorithms for lifetime maximization in wireless ad hoc networks with omni-directional and directional antennas," in *IEEE Globecom* 2006, Nov 2006, pp. 1–5.
- [40] S. Guo, M. Dong, and M. Guo, "Performance analysis of heuristic algorithms for lifetime-aware directional multicasting in wireless ad hoc networks," in 22nd International Conference on Advanced Information Networking and Applications - Workshops (aina workshops 2008), March 2008, pp. 1311–1316.
- [41] S. Guo and O. Yang, "Multicast lifetime maximization for energy-constrained wireless ad-hoc networks with directional antennas," in *Global Telecommunications Conference*, 2004. GLOBECOM '04. IEEE, vol. 6, Nov 2004, pp. 4120–4124 Vol.6.
- [42] X. Liu, S. Guo, and A. E. Saddik, "Communication complexity evaluation for longest-lived directional multicasting in wanets," in 2008 IEEE International Conference on Communications, May 2008, pp. 3029–3033.
- [43] S. Guo and O. Yang, "Formulation of optimal tree construction for maximum lifetime multicasting in wireless ad-hoc networks with adaptive antennas," in *IEEE International Conference on Communications*, 2005. ICC 2005, vol. 5, May 2005, pp. 3370–3374 Vol. 5.
- [44] —, "Improving energy efficiency for multicasting in wireless ad-hoc networks with adaptive antennas," in WiMob'2005), IEEE International Conference on Wireless And Mobile Computing, Networking And Communications, 2005., vol. 3, Aug 2005, pp. 344–351 Vol. 3.
- [45] H. Park, S. Park, T. Song, and S. Pack, "An incremental multicast grouping scheme for mmwave networks with directional antennas," *IEEE Communications Letters*, vol. 17, no. 3, pp. 616–619, March 2013.
- [46] M. Khan and M. Yuksel, "Maintaining a free-space-optical communication link between two autonomous mobiles," in 2014 IEEE Wireless Communications and Networking Conference (WCNC), April 2014, pp. 3154–3159.
- [47] M. Khan, G. Winkelmaier, and M. Yuksel, "In-band autonomous maintenance of mobile free-space-optical links: A prototype," in 2016 IEEE International Conference on Communications Workshops (ICC), May 2016, pp. 157–162.
- [48] M. Khan, M. Yuksel, and G. Winkelmaier, "Gps-free maintenance of a free-space-optical link between two autonomous mobiles," *IEEE Transactions on Mobile Computing*, vol. PP, no. 99, pp. 1–1, 2016.
- [49] S. Bhunia, M. Khan, S. Sengupta, and M. Yuksel, "Los discovery for highly directional full duplex rf/fso transceivers," in MILCOM 2016 -2016 IEEE Military Communications Conference, Nov 2016, pp. 337– 342.

- [50] M. Khan, S. Bhunia, M. Yuksel, and S. Sengupta, "Los discovery in 3d for highly directional transceivers," in MILCOM 2016 - 2016 IEEE Military Communications Conference, Nov 2016, pp. 325–330.
- [51] J. Derenick, C. Thorne, and J. Spletzer, "On the deployment of a hybrid free-space optic/radio frequency (fso/rf) mobile ad-hoc network," in 2005 IEEE/RSJ International Conference on Intelligent Robots and Systems, ser. IROS '05, Aug 2005, pp. 3990–3996.
- [52] ——, "Hybrid free-space optics/radio frequency (FSO/RF) networks for mobile robot teams," in *Multi-Robot Systems. From Swarms to Intelligent Automata*. Springer, 2005, vol. III, pp. 263 – 268.
- [53] P. LoPresti, H. Refai, J. Sluss, and I. Varela-Cuadrado, "Adaptive divergence and power for improving connectivity in free-space optical mobile networks," *Applied optics*, vol. 45, no. 25, pp. 6591–6597, 2006. [Online]. Available: https://www.osapublishing.org/abstract.cfm? uri=ao-45-25-6591
- [54] M. Bilgi and M. Yuksel, "Multi-transceiver simulation modules for free-space optical mobile ad hoc networks," *Proceedings of SPIE Defense, Security, and Sensing*, vol. 7705, p. 77050B, May 2010.
- [55] ——, "Capacity scaling in free-space-optical mobile ad hoc networks," Ad Hoc Netw., vol. 12, pp. 150–164, Jan. 2014. [Online]. Available: http://dx.doi.org/10.1016/j.adhoc.2011.12.003
- [56] A. Sevincer, M. Bilgi, M. Yuksel, and N. Pala, "Prototyping multi-transceiver free-space optical communication structures," in *Communications (ICC)*, 2010 IEEE International Conference on, ser. ICC '10, May 2010, pp. 1–5.
- [57] M. Bilgi and M. Yuksel, "Multi-element free-space-optical spherical structures with intermittent connectivity patterns," in *INFOCOM Work-shops 2008, IEEE*, ser. INFOCOM Workshops '08, April 2008, pp. 1–4.
- [58] M. Yuksel, J. Akella, S. Kalyanaraman, and P. Dutta, "Free-space-optical mobile ad hoc networks: Auto-configurable building blocks," Wireless Networks, vol. 15, no. 3, pp. 295–312, 2007. [Online]. Available: http://dx.doi.org/10.1007/s11276-007-0040-y
- [59] M. Bilgi and M. Yuksel, "Packet-based simulation for optical wireless communication," in 2010 17th IEEE Workshop on Local Metropolitan Area Networks (LANMAN), May 2010, pp. 1–6.
- [60] J. Akella, C. Liu, D. Partyka, M. Yuksel, S. Kalyanaraman, and P. Dutta, "Building blocks for mobile free-space-optical networks," in Wireless and Optical Communications Networks, 2005. WOCN 2005. Second IFIP International Conference on, ser. WOCN '05, March 2005, pp. 164–168.
- [61] M. Bilgi and M. Yuksel, "Throughput characteristics of free-space-optical mobile ad hoc networks," in *Proceedings of the 13th ACM International Conference on Modeling, Analysis, and Simulation of Wireless and Mobile Systems*, ser. MSWIM '10. New York, NY, USA: ACM, 2010, pp. 170–177. [Online]. Available: http://doi.acm.org/10.1145/1868521.1868549
- [62] A. Sevincer and M. Yuksel, "Effective transceiver selection for mobile multi-directional free-space-optical modules," in 2014 IEEE Wireless Communications and Networking Conference (WCNC), April 2014, pp. 2988–2993
- [63] B. Nakhkoob, M. Bilgi, M. Yuksel, and M. Hella, "Multi-transceiver optical wireless spherical structures for manets," *IEEE Journal on Selected Areas in Communications*, vol. 27, no. 9, pp. 1612–1622, December 2009.
- [64] Y. Jahir, M. Atiquzzaman, H. Refai, and P. G. LoPresti, "Aodvh: Ad hoc on-demand distance vector routing for hybrid nodes," in *Communications (ICC)*, 2010 IEEE International Conference on, ser. ICC '10, May 2010, pp. 1–5.
- [65] —, "Performance evaluation of aodvh: An ad hoc networking scheme for hybrid nodes," in *Computer and Information Technology (ICCIT)*, 2010 13th International Conference on, ser. ICCIT '10, Dec 2010, pp. 165–169.
- [66] R. A. Nichols, A. R. Hammons, D. J. Tebben, and A. Dwivedi, "Delay tolerant networking for free-space optical communication systems," in *Sarnoff Symposium*, 2007 IEEE, ser. IEEE Sarnoff Symposium '07, April 2007, pp. 1–5.
- [67] R. A. Nichols and A. R. Hammons, "DTN-based free-space optical and directional RF networks," in *Military Communications Conference*, 2008. MILCOM 2008. IEEE, ser. MILCOM '08, Nov 2008, pp. 1–6.
- [68] —, "Performance of DTN-based free-space optical networks with mobility," in *Military Communications Conference*, 2007. MILCOM 2007. IEEE, ser. MILCOM '07, Oct 2007, pp. 1–6.
- [69] R. A. Nichols, "Qoi in dtn-based directional networks," in 2009 IEEE Sarnoff Symposium, March 2009, pp. 1–5.
- [70] V. Navda, A. P. Subramanian, K. Dhanasekaran, A. Timm-Giel, and S. Das, "Mobisteer: Using steerable beam directional antenna for vehicular network access," in *Proceedings of the 5th International*

- Conference on Mobile Systems, Applications and Services, ser. MobiSys '07. New York, NY, USA: ACM, 2007, pp. 192–205. [Online]. Available: http://doi.acm.org/10.1145/1247660.1247684
- [71] A. Spyropoulos and C. S. Raghavendra, "Energy efficient communications in ad hoc networks using directional antennas," in Proceedings. Twenty-First Annual Joint Conference of the IEEE Computer and Communications Societies, vol. 1, 2002, pp. 220–228 vol.1.
- [72] O. Awwad, A. Al-Fuqaha, B. Khan, and G. B. Brahim, "Topology control schema for better qos in hybrid rf/fso mesh networks," *IEEE Transactions on Communications*, vol. 60, no. 5, pp. 1398–1406, May 2012.
- [73] R. R. Choudhury, X. Yang, R. Ramanathan, and N. H. Vaidya, "On designing mac protocols for wireless networks using directional antennas," *IEEE Transactions on Mobile Computing*, vol. 5, no. 5, pp. 477–491, May 2006.
- [74] R. R. Choudhury and N. H. Vaidya, *Impact of Directional Antennas on Ad Hoc Routing*. Berlin, Heidelberg: Springer Berlin Heidelberg, 2003, pp. 590–600. [Online]. Available: http://dx.doi.org/10.1007/978-3-540-39867-7\_57
- [75] G. Zhang, Y. Xu, X. Wang, X. Tian, J. Liu, X. Gan, H. Yu, and L. Qian, "Multicast capacity for vanets with directional antenna and delay constraint," *IEEE Journal on Selected Areas in Communications*, vol. 30, no. 4, pp. 818–833, May 2012.
- [76] R. R. Choudhury, X. Yang, R. Ramanathan, and N. H. Vaidya, "Using directional antennas for medium access control in ad hoc networks," in *Proceedings of the 8th Annual International Conference on Mobile Computing and Networking*, ser. MobiCom '02. New York, NY, USA: ACM, 2002, pp. 59–70. [Online]. Available: http://doi.acm.org/10.1145/ 570645.570653
- [77] T. ElBatt, T. Anderson, and B. Ryu, "Performance evaluation of multiple access protocols for ad hoc networks using directional antennas," in 2003 IEEE Wireless Communications and Networking, 2003. WCNC 2003., vol. 2, March 2003, pp. 982–987 vol.2.
- [78] Z. Huang, C.-C. Shen, C. Srisathapornphat, and C. Jaikaeo, "A busy-tone based directional mac protocol for ad hoc networks," in MILCOM 2002. Proceedings, vol. 2, Oct 2002, pp. 1233–1238 vol.2.
- [79] Y.-B. Ko, V. Shankarkumar, and N. H. Vaidya, "Medium access control protocols using directional antennas in ad hoc networks," in *Proceedings IEEE INFOCOM 2000. Conference on Computer Communications. Nineteenth Annual Joint Conference of the IEEE Computer and Communications Societies (Cat. No.00CH37064)*, vol. 1, 2000, pp. 13–21 vol.1.
- [80] R. Ramanathan, "On the performance of ad hoc networks with beamforming antennas," in *Proceedings of the 2Nd ACM International Symposium on Mobile Ad Hoc Networking &Amp; Computing*, ser. MobiHoc '01. New York, NY, USA: ACM, 2001, pp. 95–105. [Online]. Available: http://doi.acm.org/10.1145/501426.501430
- [81] R. Ramanathan, J. Redi, C. Santivanez, D. Wiggins, and S. Polit, "Ad hoc networking with directional antennas: a complete system solution," *IEEE Journal on Selected Areas in Communications*, vol. 23, no. 3, pp. 496–506, March 2005.
- [82] I. Rubin, Y. Y. Lin, A. Baiocchi, F. Cuomo, and P. Salvo, "Vehicular backbone networking protocol for highway broadcasting using directional antennas," in 2013 IEEE Global Communications Conference (GLOBECOM), Dec 2013, pp. 4414–4419.
- [83] S. Kuribayashi, Y. Sakumoto, H. Ohsaki, S. Hasegawa, and M. Imase, "Performance evaluation of epidemic broadcast with directional antennas in vehicular ad-hoc networks," in 2011 IEEE/IPSJ International Symposium on Applications and the Internet, July 2011, pp. 260–265.
- [84] C. Jaikaeo and C. C. Shen, "Multicast communication in ad hoc networks with directional antennas," in *Proceedings*. 12th International Conference on Computer Communications and Networks (IEEE Cat. No.03EX712), Oct 2003, pp. 385–390.
- [85] A. K. Das, R. J. Marks, M. El-Sharkawi, P. Arabshahi, and A. Gray, "Optimization methods for minimum power multicasting in wireless networks with sectored antennas," in 2004 IEEE Wireless Communications and Networking Conference (IEEE Cat. No.04TH8733), vol. 3, March 2004, pp. 1299–1304 Vol.3.
- [86] S. Guo, O. Yang, and V. Leung, "Joint optimization of energy consumption and antenna orientation for multicasting in static ad hoc wireless networks," *IEEE Transactions on Wireless Communications*, vol. 5, no. 9, pp. 2563–2568, September 2006.
- [87] M. E. Steenstrup, "Exploiting directional antennas to provide quality of service and multipoint delivery in mobile wireless networks," in *IEEE Military Communications Conference*, 2003. MILCOM 2003., vol. 2, Oct 2003, pp. 987–992 Vol.2.

- [88] K. Sundaresan, K. Ramachandran, and S. Rangarajan, "Optimal beam scheduling for multicasting in wireless networks," in *Proceedings of* the 15th Annual International Conference on Mobile Computing and Networking, ser. MobiCom '09. New York, NY, USA: ACM, 2009, pp. 205–216. [Online]. Available: http://doi.acm.org/10.1145/1614320. 1614343
- [89] A. K. Majumdar and J. C. Ricklin, Free-Space Laser Communications, Principles and Advances. Springer, 2008.
- [90] V. V. Vazirani, Approximation Algorithms. Springer, 2003.
- [91] E. Balas, "The prize collecting traveling salesman problem: Ii. polyhedral results," *Networks*, vol. 25, no. 4, pp. 199–216, 1995. [Online]. Available: http://dx.doi.org/10.1002/net.3230250406
- [92] —, "The prize collecting traveling salesman problem," *Networks*, vol. 19, no. 6, pp. 621–636, 1989. [Online]. Available: http://dx.doi.org/10.1002/net.3230190602
- [93] Egon Balas and Clarence H. Martin, "combinatorial optimization in steel rolling." DIMACS Technical Report 91-18/RUTCOR Report 3-91, Apr. 1991, pp. 20–24.
- [94] G. Hardy and E. Wright, An Introduction to the Theory of Numbers, 5th ed. Oxford University Press, 1979.
- [95] L.-P. Bigras, M. Gamache, and G. Savard, "The time-dependent traveling salesman problem and single machine scheduling problems with sequence dependent setup times," *Discrete Optimization*, vol. 5, no. 4, pp. 685 – 699, 2008. [Online]. Available: http://www. sciencedirect.com/science/article/pii/S1572528608000339
- [96] J.-C. Picard and M. Queyranne, "The time-dependent traveling salesman problem and its application to the tardiness problem in one-machine scheduling," *Oper. Res.*, vol. 26, no. 1, pp. 86–110, Feb. 1978. [Online]. Available: http://dx.doi.org/10.1287/opre.26.1.86

PLACE PHOTO HERE Michael Atakora received the B.Sc. degree in telecommunications engineering from Kwame Nkrumah University of Science and Technology, Ghana, in 2010, the M.Sc degree in electrical engineering from Tuskegee University, USA in 2013. He is currently working toward the Ph.D degree in electrical engineering and computer science under the guidance of Dr. Harsha Chenji at Ohio University, USA, where his primary research interest is in hybrid RF/FSO mobile adhoc networks.

PLACE PHOTO HERE Harsha Chenji Harsha Chenji received the B.Tech. degree in electrical and electronics engineering from NITK Surathkal, India, in 2007, and the M.S. and Ph.D. degrees in computer engineering from Texas A&M University, in 2009 and 2014, respectively, advised by Prof. R. Stoleru. In 2014, he joined as a Post-Doctoral Researcher with the Wireless Networks Laboratory, headed by Prof. Z. J. Haas, Department of Computer Science, The University of Texas at Dallas. Since 2015, he has been an Assistant Professor with the School of Electrical Engineering

and Computer Science, Ohio University, where he leads the Wireless Systems Research Group. His general area of research is computer networking. His current research interests include free-space optical networks and wireless networks. In 2016, he was selected for the 2016 Visiting Faculty Research Program by the Air Force Research Laboratory (Information Directorate), Rome, NY, USA.